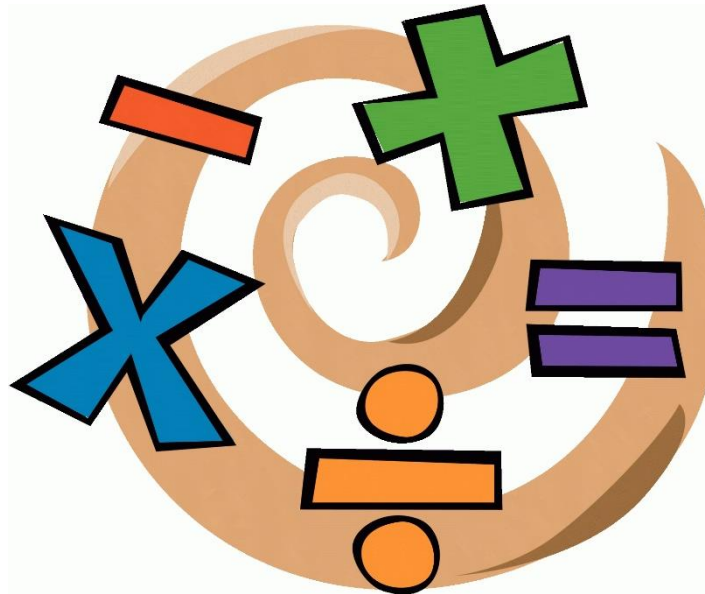




Written Calculation Methods
Middleton Primary School

ADDITION

SUBTRACTION



MULTIPLICATION

DIVISION

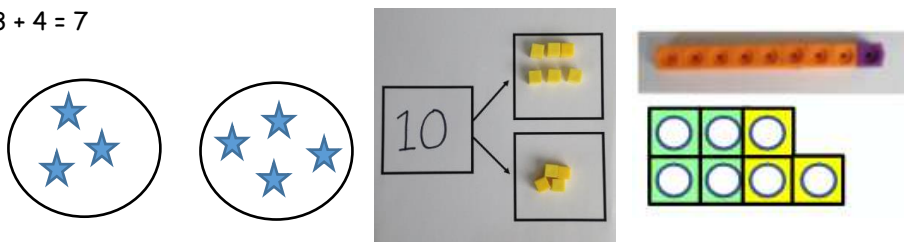
Written Methods Policy - Middleton Primary School - ADDITION

Step 1

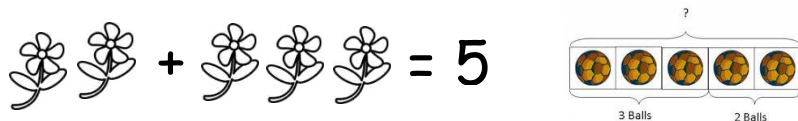
Use songs and rhymes that include counting on, such as "1, 2, 3, 4, 5, Once I Caught a Fish Alive".
Add by using jottings to draw objects then find out how many there are altogether.
Add by mentally retaining a number and using fingers to count on.
Add numbers together by counting on using a number line.

Concrete

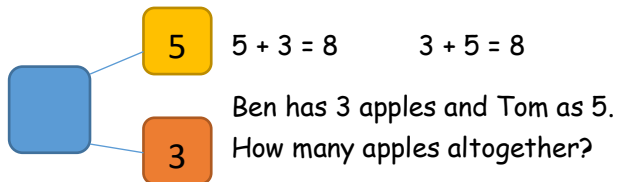
$$3 + 4 = 7$$



Pictorial



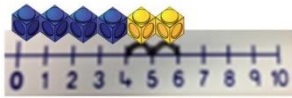
Abstract



Step 2

Add numbers together by counting on
Add 10 to a number by moving down one square.

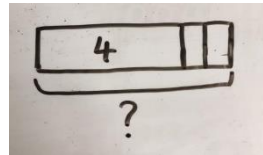
Concrete



Pictorial

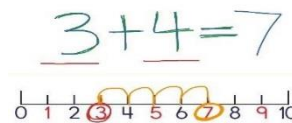
$$24 + 5 =$$

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Abstract

What is 4 more than 7?



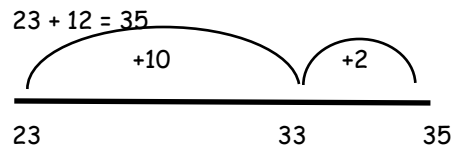
Children place larger number in their head and count on mentally, using their fingers or using jottings.

$$7 + 4 = 11$$

$$\text{IIIIII} + \text{IIII} = 11$$

Step 3

Add numbers together by counting on using a blank number line, initially jumping in 1's but extending to jumping in 10's and 1's.

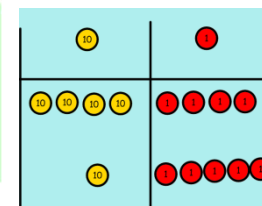
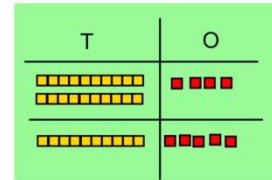
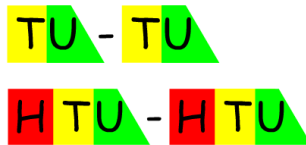
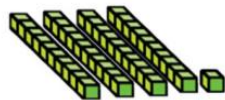


Step 4
(NO REGROUPING)

Partition into hundreds, tens and ones and recombine.

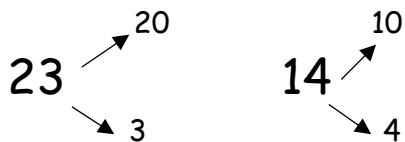
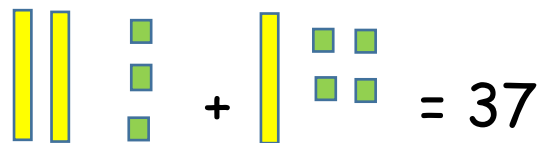
Concrete

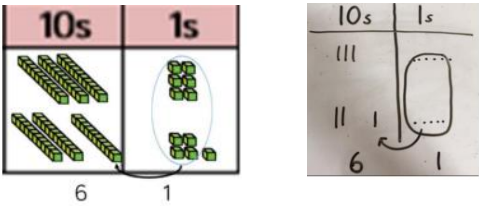
$41 + 8 = 49$



Pictorial

Use drawings to support partitioning and understanding of place value.



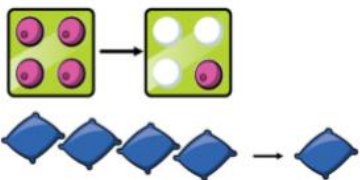
	<p>Abstract</p> <p>Use expanded column addition to add 3-digit numbers.</p> $ \begin{array}{r} \begin{array}{c} \text{H} \quad \text{T} \quad \text{O} \\ 3 \quad 6 \quad 4 \\ + 2 \quad 7 \quad 8 \\ \hline 1 \quad 1 \quad 2 \\ 1 \quad 3 \quad 0 \\ + 5 \quad 0 \quad 0 \\ \hline 6 \quad 4 \quad 2 \end{array} \end{array} $
<p>Step 5 Regrouping</p>	<p>Concrete/pictorial</p> <p>Using Base 10 or place value counters, make both numbers on the place value grid. Add up the ones and exchange 10 ones for 1 ten. Carry it over to the tens column.</p>  <p>Use shorter column method</p> $ \begin{array}{r} 1499 \\ + 1123 \\ \hline 2622 \\ 11 \end{array} $
<p>Step 6</p>	<p>Use column addition to add whole numbers and decimals.</p> $ \begin{array}{r} 1628.9 \\ + 117.25 \\ \hline 1746.15 \\ 11 \end{array} $

Written Methods Policy - Middleton Primary School - SUBTRACTION

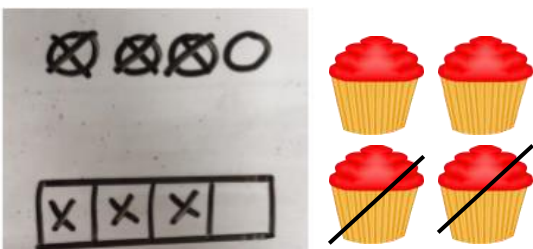
Step 1

Use songs and rhymes that include counting back, such as Five Little Speckled Frogs, Five Little Men in a Flying Saucer and Ten Sizzling Sausages. Subtract by mentally retaining a number and using fingers to count back.

Concrete



Pictorial

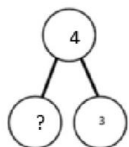


Abstract

$$4 - 3 =$$

$$\square = 4 - 3$$

4	
3	?

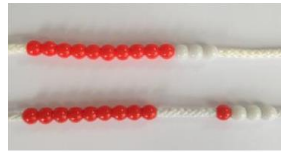
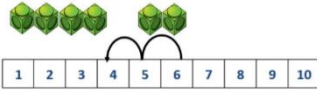


Step 2

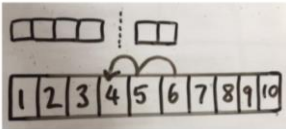
Counting back

Concrete

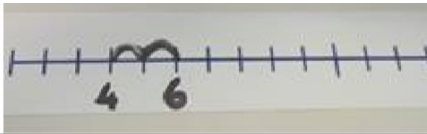
$$6 - 2 = 4$$



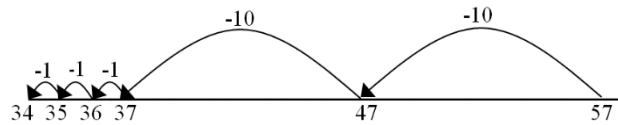
Pictorial



Abstract

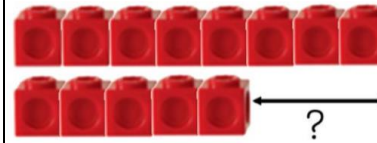


This can progress up to counting back 2 digit numbers.



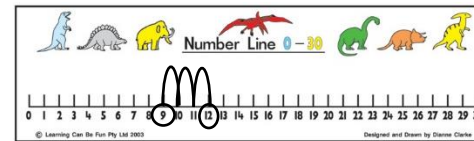
Counting on

Concrete



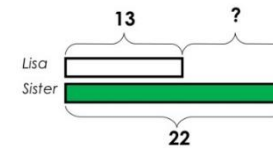
Pictorial

$$12 - 9 =$$



Abstract - bar model

Lisa is 13 years old. Her sister is 22 years old.
Find the difference in age between them.



Step 3

Use of mental subtraction - getting to the nearest 10

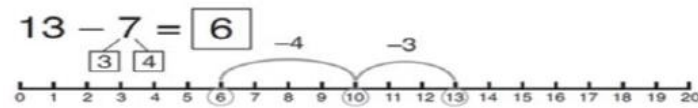
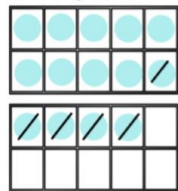
concrete

$$14 - 5 =$$



Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.

pictorial



abstract

$$\begin{array}{r} 14 - 5 = 9 \\ \quad \swarrow \quad \searrow \\ \quad 4 \quad \quad 1 \end{array}$$

$$14 - 4 = 10$$

$$10 - 1 = 9$$

Step 4
(NO REGROUPING)

Pictorial
 $35 - 13 = 22$

Reinforce place value so the children understand that it is $30 - 10$ and not $3 - 1$.

Abstract

If needed, partition the number to reinforce $40 - 20$ instead of $4 - 2$.

$$47 - 24 = 23$$

$$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$$

Simple written column method.

	4	8
-		7
	4	1

Step 5

Subtract using methods including borrowing

$$2436 - 1237 = 12019$$

$$\begin{array}{r} 2\ 4\ 3\ \overset{3}{4}\ \overset{16}{6} \\ -1\ 2\ 3\ 2\ 7 \\ \hline 1\ 2\ 0\ 1\ 9 \end{array}$$

Step 6

Apply to decimals

$$1628.90 - 117.25 = 1511.65$$

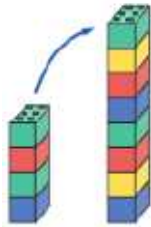
$$\begin{array}{r} 1628.\overset{80}{9} \\ - 117.25 \\ \hline 1511.65 \end{array}$$

Written Methods Policy - Middleton Primary School - MULTIPLICATION

Step 1

Double numbers using objects in role play and practical contexts.

concrete



double 4 is 8

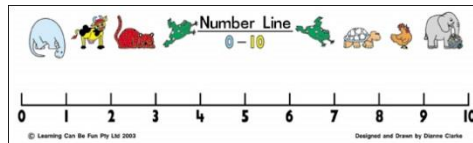
$$4 \times 2 = 8$$

pictorial

Use jottings/number line to find the double of numbers.

$$4 + 4 =$$

. .
. .
. .
. .



Step 2

Multiplication of 2s 5s and 10s

Concrete



pictorial

Calculate answers by drawing pictures. E.g. finding how many eyes on 3 people



Abstract

Use of number line or timestable knowledge

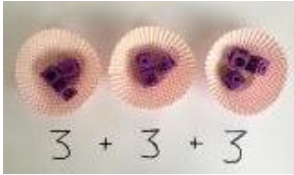
+2 +2 +2 +2



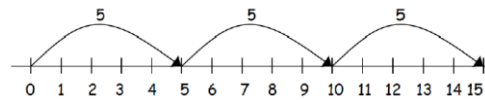
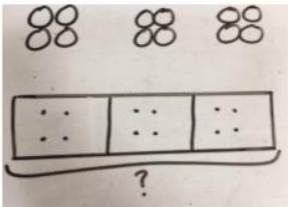
0 2 4 6 8

Step 3

Repeated addition
Concrete



Pictorial



$$5 + 5 + 5 = 15$$

abstract

From this, using their times table recall.

Step 4

Arrays
concrete



pictorial



$$4 \times 2 = 8$$

$$2 \times 4 = 8$$



$$2 \times 4 = 8$$

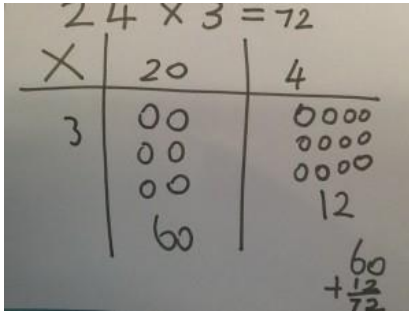
$$4 \times 2 = 8$$

Step 5

Grid method

Pictorial

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below



Abstract

X	30	5
7	210	35

$$210 + 35 = 245$$

X	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Add up each row and then add them together.

Step 6

Column method:

Step back - partition if needed

$$\begin{array}{r} 37 \\ \times 5 \\ \hline 35 \text{ (7 \times 5)} \\ 150 \text{ (30 \times 5)} \\ \hline 180 \end{array}$$

Multiply numbers using the column method.

$$\begin{array}{r} 1632 \\ \times 7 \\ \hline 11424 \\ 421 \\ \hline \end{array}$$

$$\begin{array}{r} 1632 \\ \times 87 \\ \hline 11424 \\ 421 \\ \hline \end{array}$$

$$\begin{array}{r} 130560 \\ \times 521 \\ \hline \end{array}$$

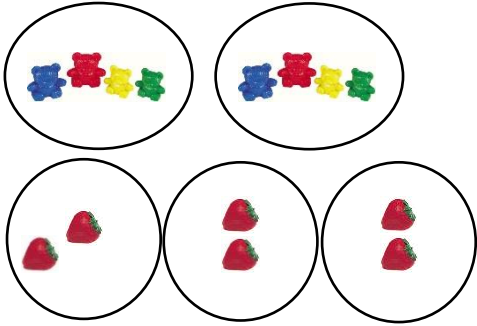
$$\begin{array}{r} 141984 \\ \hline \end{array}$$

$$\begin{array}{r} 3.26 \\ \times 3 \\ \hline 9.78 \\ 1 \end{array}$$

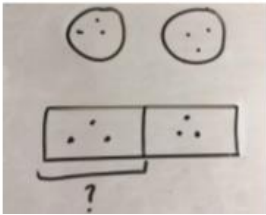
Written Methods Policy - Middleton Primary School - DIVISION

Step 1

Find half by sharing an even number over objects into two groups and then equal groups
concrete



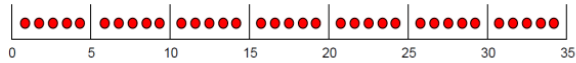
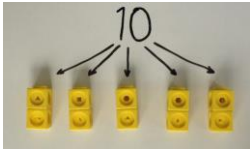
Pictorial



Abstract
Using number sentences
 $4 \div 2 = 2$

Step 2

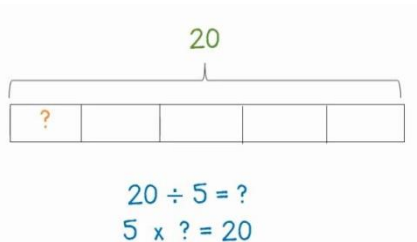
Grouping numbers
Concrete



$$96 \div 3 = 32$$



Pictorial



Abstract

Using number sentences

Using multiplication facts to support division

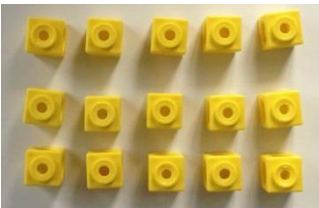
Step 3

Using arrays to support the ability to do inverse.

Eg $15 \div 3 = 5$ $5 \times 3 = 15$

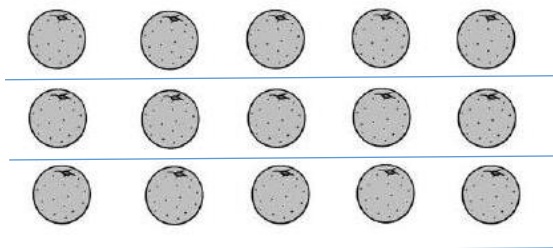
$15 \div 5 = 3$ $3 \times 5 = 15$

Concrete



Pictorial

Draw an array and use lines to split the array into groups to make multiplication and division sentences.



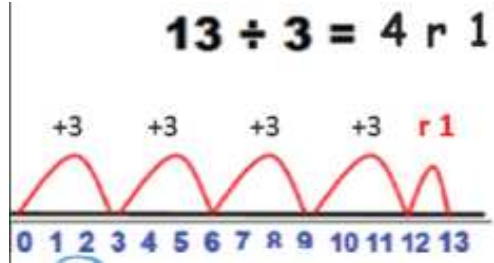
Abstract

Writing the number sentences using their timestables knowledge

Step 4

Introduction of remainders

Pictorial



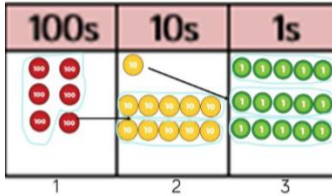
Abstract

writing the number sentence with the remainder

Step 5

Bus stop method - only using up to 12
Concrete/pictorial

$$615 \div 5$$



1. Make 615 with place value counters.
2. How many groups of 5 hundreds can you make with 6 hundred counters?
3. Exchange 1 hundred for 10 tens.
4. How many groups of 5 tens can you make with 11 ten counters?
5. Exchange 1 ten for 10 ones.
6. How many groups of 5 ones can you make with 15 ones?

Abstract

Begin with calculations with no remainders.

$$\begin{array}{r} 218 \\ 4 \overline{) 872} \end{array}$$

Move onto calculations with remainders.

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \end{array}$$

Step 6

Represent the remainder as a fraction

Long division

Maria buys a yearly train pass for £2,799. She uses it for a total of 45 weeks. How much does it cost her to travel by train each week?

- Read the question and read it again. What is it asking?
I have to divide 2,799 by 45.
- Look at the numbers and make an estimate.
 $2,800 \div 50$ is a bit more than 56.
- Start by dividing 279 by 45 to find how many times 45 goes into 279.
Write 6 in the answer space and record 270
(45×6) below 279 so the remainder can be found.
- Bring down the digit 9.
Divide 99 by 45 to find out how many times 45 goes into 99.
Write 2 in the answer space and record 90 (45×2) below 99 so the remainder can be found.
- A remainder must be shown as a decimal for the context of money.
As no more whole 'lots of 45' go into 9, put a decimal point and a zero next to 2,799 and in the answer space.
Bring down the zero as before.
- What is your answer? Use two decimal places for money.
£62.20

Decimals

$$\begin{array}{r}
 14.6 \\
 35 \overline{) 511.0} \\
 \underline{35} \\
 16 \\
 \underline{16} \\
 0 \\
 \underline{0} \\
 0
 \end{array}$$